

# Class VII Chapter-3

## RATIONAL NUMBERS



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# Rational numbers



- Any number that can be expressed in the form of  $p/q$  where  $p$  and  $q$  are integers and  $q$  is not equal to 0 is called a rational number.
- The set of rational numbers is denoted by  $Q$ .
- Every natural number is a rational number.
- E.g  $4=4/1$
- Every whole number is a rational number.
- Eg  $0= 0/1$

# Rational numbers



- Every integer is a rational number
- Eg:  $-5 = -5/1$
- Every fraction is a rational number
- Eg :  $4/13$
- Positive rational number: if both numerator and denominator are positive or both are negative.
- Eg:  $-5/-7$  or  $5/7$

# Rational numbers



- **Negative rational numbers**
- In this either numerator or denominator is negative
- Eg:  $-7/9$  or  $7/-9$
- We can represent rational numbers on the number line.

# Assignment -1



- Solve ex 3.1 OF WOW MATHEMATICS CLASS VII in your register.
- **NOTE: KINDLY DOWNLOAD THE BOOK.**

# Rational number in standard form



- A rational number is said to be in **standard form** if  $q > 0$  and  $p$  and  $q$  are co-prime means they have no common factor except 1.
- Eg:  $-15/45$  in standard form is  $-1/3$
- $32/-60$  in standard form is  $-8/15$
- Note: minus sign is always in the numerator in standard form.

# Assignment -2



- 1. Convert into standard form;
- $-\frac{3}{33}$
- $\frac{40}{-25}$
- $\frac{17}{-56}$
- $\frac{51}{26}$

# Equivalent rational numbers



- If any two rational numbers can be reduced to the same standard form, then they are equivalent rational numbers.
- For eg:  $-10/11$  and  $-30/33$  are equivalent rational numbers.
- $-10/11$  has no common factor except one.
- $-30/33 = -3 \times 10 / 3 \times 11 = -10/11$  also has no common factor except one after reducing.

# TRY NOW



- Write two equivalent rational numbers of
- 1.  $-60/66$
- 2.  $14/56$
- 3.  $4/5$

# Absolute value of a rational number



- Absolute value of a rational number is its numerical value regardless of sign.
- For eg : absolute value of  $-7/13$  is  $7/13$
- Symbol of absolute value is  $| \quad |$ .
- $| 7/8 | = 7/8$
- $| -7/8 | = 7/8$

# RATIONAL NUMBERS BETWEEN TWO RATIONAL NUMBERS



- **NOTE:** There are infinite rational numbers between two given rational numbers.
- To insert rational numbers between two given rational numbers.
- Make the denominators same.
- Second: multiply with  $(n+1)$  where  $n$  is the number of rational numbers to be inserted.

# example



- Insert **six** rational numbers between  $\frac{1}{2}$  and  $\frac{5}{8}$ .
- $\frac{1}{2} = 1 \times \frac{4}{2} \times \frac{4}{4} = \frac{4}{8}$
- $4 \times \frac{7}{8} \times \frac{7}{7} = \frac{28}{56}$
- $5 \times \frac{7}{8} \times \frac{7}{7} = \frac{35}{56}$  (note: we have taken number 7 as we have to insert 6 rational numbers, so we multiply with  $(n+1)$ )
- **$(\frac{28}{56}, \frac{29}{56}, \frac{30}{56}, \frac{31}{56}, \frac{32}{56}, \frac{33}{56},$**
- **$\frac{34}{56}, \frac{35}{56})$**

# Assignment -3



- Insert six rational numbers between  $\frac{5}{7}$  and  $\frac{4}{3}$ .
- Find absolute value of:
  - $|\frac{3}{6}| =$
  - $|\frac{-9}{24}| =$
  - $|\frac{-7}{45}| =$

# Comparing and ordering of rational numbers



- We can compare rational numbers by making their denominators same and then we can arrange them in ascending or descending order.
- Note: if minus sign is in the denominator, take it in the numerator, and then solve as usual.

# Assignment-4



- Compare the two given rational numbers:
- $-11/20$  and  $5/-14$
- Arrange the rational numbers in ascending order:
- $7/11$ ,  $8/-6$ ,  $-6/8$ ,  $27/25$
- Find  $x$  :  $15/x = -5/4$
- (Hint: cross multiply)

# OPERATION ON RATIONAL NUMBERS



- Addition : we add rational numbers by making the denominator same.
- Subtraction : we follow the same rule for subtraction.
- Additive inverse: every rational number has it's additive inverse. eg: additive inverse of  $\frac{5}{9}$  is  $-\frac{5}{9}$ .

# worksheet



- Add  $2/3$  and  $-4/5$
- Ans  $-2/15$
- Subtract  $7/9$  from  $5/9$ .
- Hint:  $5/9 - 7/9$  Ans  $-2/9$
- What is additive inverse of  $-9/24$ ?

# MULTIPLICATION AND RECIPROCAL



- To multiply rational numbers, we multiply numerator with numerator and denominator with denominator.
- Eg:  $\frac{3}{7} \times \frac{-5}{9} = \frac{-3 \times 5}{7 \times 9} = \frac{-15}{63}$
- **Reciprocal:** reciprocal of a rational number is found by interchanging numerator and denominator.
- Fr eg: reciprocal of  $\frac{7}{8}$  is  $\frac{8}{7}$

# WORKSHEET



- Multiply:
- $56/7 \times 9/23$
- $4/5 \times 17/8$
- Find reciprocal of :
- $45/-23$
- $-78/57$
- $3/4$

# DIVISION



- To divide a given rational number by another non zero rational number, we convert divide sign into multiply and reciprocate the right hand side number.
- Fr eg:  $\frac{2}{3} \div \frac{4}{5}$
- Solution:
- $\frac{2}{3} \times \frac{5}{4} = \frac{10}{12} = \frac{5}{6}$

# Word problem



- Product of two rational numbers is  $18/35$ . If one of them is  $-2/5$ , find the other?
- Solution:
- $a \times b = c$
- $-2/5 \times b = 18/35$
- $b = 18/35 \div -2/5$
- $b = 18/35 \times 5/-2 = 90/-70 = -9/7$

# Try me



- Product of two rational numbers is  $\frac{27}{56}$ . If one of the rational number is  $-\frac{3}{7}$ , find the other?  
Ans:  $-\frac{9}{8}$
- Krati finished  $\frac{1}{3}$  of her assignment on the first day and  $\frac{1}{4}$  of the assignment on the second day. What part of the assignment is yet to be finished?
- Hint: add  $\frac{1}{3}$  and  $\frac{1}{4}$ , then subtract the result from 1.